A growing literature on poverty traps emphasizes the links between multiple equilibria and risk avoidance. However, multiple equilibria may also foster risk-taking behavior by some poor people. We illustrate this idea with a simple analytical model in which people with different wealth and ability endowments make investment and risky activity choices in the presence of known nonconvex asset dynamics. This model underscores a crucial distinction between familiar static concepts of risk aversion and forward-looking dynamic risk responses to nonconvex asset dynamics. Even when unobservable preferences exhibit decreasing absolute risk aversion, observed behavior may suggest that risk aversion actually increases with wealth near perceived dynamic asset thresholds. Although high ability individuals are not immune from poverty traps, they can leverage their capital endowments more effectively than lower ability types and are therefore less likely to take seemingly excessive risks. In general, linkages between behavioral responses and wealth dynamics often seem to run in both directions. Both theoretical and empirical poverty trap research could benefit from making this two-way linkage more explicit. (JEL D81, O12, D90)
rather than consumption, for those at or just above the threshold at which wealth dynamics bifurcate (Barrett et al. 2006; Carter et al. forthcoming; Hoddinott 2006; McPeak 2004; Zimmerman and Carter 2003). The intuition behind such asset smoothing is simple: people safeguard the productive assets on which their future livelihood depends if liquidating assets so as to smooth consumption pushes them below a threshold at which they expect exogenous asset dynamics to suddenly cause further asset loss. The difference between these two views has important implications for behavior under risk. Whereas the first sees causation running from risk preferences to wealth dynamics, the second suggests it might run from wealth dynamics to risk preferences as manifest in risk-taking behaviors. This paper develops this latter, largely overlooked point.

By suggesting that risk-taking behavior might be shaped by wealth dynamics, the asset smoothing hypothesis—that agents become extremely averse to loss of productive assets in the presence of thresholds at which wealth dynamics bifurcate—raises an intriguing, complementary possibility: multiple equilibria associated with nonconvex asset dynamics could lead to seemingly excessive risk-taking behavior among those subjacent to a dynamic asset threshold. Such individuals might take chances when a safe strategy is unlikely to break them out of a poverty trap and financial market failures preclude a more conventional investment-based strategy for accumulating capital and exiting poverty.

This observation is not exactly new, but explanations for this behavior have previously relied on unconventional preferences, typically with embedded and implicit wealth dynamics. Most famously, Friedman and Savage (1948) motivated their double inflection, “wiggly” utility curve with a loose reference to implicit wealth dynamics that makes it difficult for individuals to move to higher socioeconomic classes and hence risk seeking when upside payoffs allow them to move to a higher class. In their words, “the segments of diminishing marginal utility correspond to socioeconomic classes, the segment of increasing marginal utility to a transitional stage between a lower and a higher socioeconomic class” (page 304). Others subsequently explored these underlying dynamics slightly more explicitly but continued to embed them in preferences. Many of these earlier models foreshadow some of the key features of the multiple equilibria models of the 1990s, namely, indivisible human capital investments (Yew Kwang 1965), credit market imperfections (Hakansson 1970; Masson 1972), and nutritional subsistence constraints (Kunreuther and Wright 1979; Masson 1974; Roumasset 1976).

With the benefit of recent work on poverty dynamics, Banerjee (2004) addresses asset dynamics more explicitly by contrasting poverty above dynamic asset thresholds (vulnerability) with poverty below these thresholds (desperation), a characterization somewhat similar to ours. His perspective is based, however, on proximity to a lower utility bound and posits that risk taking may be greatest for the very poorest. By contrast, our model explains risk taking as a constrained optimal choice for those poor who are near the asset threshold but otherwise blocked by credit constraints from accumulating the capital necessary to escape the poverty trap. The literature has thus far overlooked the intuitive point that thresholds associated with nonconvexities that generate poverty traps might induce risk taking among a specific subpopulation—the poor who are subjacent to the threshold—for whom gambles may provide a mechanism for (probabilistic) wealth accumulation when credit- or savings-based investment is infeasible. This paper therefore considers how the existence of thresholds in the laws of motion describing asset dynamics in multiple equilibrial systems might induce extraordinary risk taking by certain subpopulations among the poor and how risky behavior might vary according to latent ability endowments.

We illustrate these ideas with a simple analytical model in which people make activity and investment choices. One activity involves timeless risk with zero expected return. Investment inherently trades lower current consumption for higher future consumption. While no risk averse agent would engage in the risky activity under standard assumptions, we show that risk taking occurs and is optimal and nonmonotonically related to liquid wealth within a key asset range when nonconvex asset dynamics characterize the system. Indeed, among those who take on seemingly excessive risk, wealth and risk taking are inversely related even when preferences exhibit decreasing absolute risk aversion. The core intuition is that some people will take chances so as to avoid predictable collapse if not taking chances leads them deeper into a trap. If agents perceive the underlying asset dynamics in a given setting, observable behavior under
risk may be shaped simultaneously by static risk preferences and dynamic risk responses conditioned by the law of motion for wealth. This analysis therefore carries implications for the empirical estimation of risk preferences and the oft-maintained assumption of a monotone relation between risk premia and wealth.

II. THE MODEL

Suppose that individuals have a strictly concave, contemporaneous utility function defined over consumption \( c \geq 1 \) as \( u(c) = \ln(c) \) and live for two periods. Intertemporally additive utility for these two periods is given by \( U(c_1, c_2) = u(c_1) + \delta u(c_2) \), where \( 0 < \delta < 1 \) is a discount factor. Individuals have three initial endowments. \( W \) is unproductive liquid wealth (including food), which can be stored or consumed but does not generate any flow of real income. \( H_1 \) is illiquid, productive wealth (e.g., human capital), which generates income without depreciation as long as consumption is sufficient. Finally, individuals are endowed with a discount factor. Individuals have three choice variables: \( c_t \) is consumption, \( K \) represents investment of \( W \) in future productive wealth with rate of return \( s > 0 \) such that \( H_2 = H_1 + sK \), and \( Y \) is the allocation of \( W \) to a fair coin-toss gamble (i.e., zero expected value) that pays \( 2Y \) in period \( t = 1 \) with probability \( p = 1/2 \) and 0 otherwise.

Without loss of generality, we capture wealth dynamics in this simple model with a single, stark consumption threshold \( \overline{c} \). We assume that (a) if \( c_1 < \overline{c} \), then \( H_2 = r_1^{-1} \) (instead of \( H_2 = H_1 + sK \)) so that \( r_1 H_2 = 1 \) and (b) \( r_L > H_1^{-1} \) so that \( r_1 H_2 > 1 \forall i \) if \( c_1 \geq \overline{c} \). These assumptions ensure that \( u(r_1 H_2 | c_1 < \overline{c}) = 0 < u(r_1 H_2 | c_1 \geq \overline{c}) \), implying that insufficient consumption can be understood as permanent disability (in the limit, death). We assume for simplicity that individuals choose \( K \) and \( Y \) and observe the outcome of the coin toss before choosing \( c_1 \). While we assume that any liquid wealth not consumed in Period 1 carries over to Period 2, agents face a positive discount rate, no return on liquid wealth, and no incentive for precautionary saving and thus have no reason to store up liquid wealth for Period 2. The expected utility model implied by this set up is:

\[
\begin{align*}
\max_{Y \in [0, W]} \max_{K \in [0, W]} & \quad E[U(c_1, c_2)] \\
\text{s.t.} & \quad Y + K \leq W \\
& \quad c_1 \leq W + \tilde{y} + r_1 H_1 - K \\
& \quad c_2 \leq W + \tilde{y} + r_1 H_1 - K - c_1 + r_1 H_2 \\
& \quad H_2 = \begin{cases} H_1 + sK & \text{if } c_1 \geq \overline{c} \\ r_1^{-1} & \text{if } c_1 < \overline{c} \end{cases} \\
& \quad \tilde{y} = \begin{cases} 2Y & p = 1/2 \\ 0, & 1 - p = 1/2 \end{cases}
\end{align*}
\]

The threshold \( \overline{c} \) creates an important nonconvexity in asset dynamics, as the discontinuous law of motion for productive wealth generates multiple dynamic equilibria, with a lower stable dynamic equilibrium at \( H = r_1^{-1} \). This simple dynamic asset threshold effectively links Periods 1 and 2 in such a way that for some parameter values there is a stark divergence between standard static risk preferences, as reflected in the (unobservable) Arrow-Pratt coefficient of absolute risk aversion \((-u''/u')\), and what might be termed a “dynamic risk response” as reflected in observed risk-taking behavior given agent knowledge of the prevailing asset dynamics of the system. That is, some individuals will risk a portion of their wealth in a way that seems contrary to their risk averse preferences in an attempt to survive until Period 2.

To solve the model, consider three cohorts of individuals: (A) a hopelessly trapped cohort, (B) a desperate cohort of individuals for whom the gamble is their only hope for survival, and (C) a richer cohort that is safely above the consumption threshold. Individuals in all three cohorts are Arrow-Pratt risk averse with a (static) coefficient of absolute risk aversion \( u''/u' = 1/c > 0 \). Because the timeless gamble has an expected payoff of zero, they will choose \( Y^* > 0 \) if and only if winning the gamble brings some benefit in addition to the direct monetary value of the win—namely, preservation of productive assets into Period 2. This is only true for individuals whose initial endowments satisfy the following two conditions: (1) \( W + r_1 H_1 < \overline{c} \) and (2) \( 2W + r_1 H_1 \geq \overline{c} \). The first condition ensures that individual \( i \)'s consumption will be insufficient if he ignores the coin-toss opportunity; the second ensures that a bet of \( Y = W \) (or
less if condition (ii) holds with strict inequality) will provide a 50:50 chance of reaching the consumption threshold, $\bar{c}$. Together, these two conditions define cohort B as individuals for whom the coin toss is their only chance to escape otherwise-certain penury. Initial endowments in the trapped cohort A satisfy condition (i) but not (ii); even an “all or nothing” bet of $W$ offers no hope of preserving $H_1$. Initial endowments in the richer cohort C satisfy condition (ii) but not (i) such that asset retention is guaranteed. Finally, note that these cohort conditions are not only defined by wealth but also conditioned on ability.

Cohorts A, B, and C in this model are depicted graphically in $H_1$ and $W$ space in Figure 1. To capture the effect of ability on risk-taking behavior, we depict the boundaries of behavior for each cohort as mapped out by the highest ability ($r_{1H}$) and lowest ability ($r_{1L}$) individuals in these cohorts. The obtuse triangles depict cohort B’s initial endowment range in $H_1$ and $W$ space; the smaller, cross-hatched triangle represents highest ability individuals, whereas the shaded triangle represents lowest ability individuals. Cohort A (cohort C) encompasses highest and lowest ability individuals with initial endowments southwest (northeast) of these respective triangles. Note that the boundary between cohorts A and B in Figure 1 is a function not just of initial asset and ability endowments but also of the odds offered on the gamble. Gambles with worse than 50:50 odds would offer a possible escape route from long-term poverty to those who otherwise face certain asset loss, creating profit-taking opportunities for those who offer such gambles to the poor. In particular, if the gamble paid $nY$ with probability $1/n$ and 0 otherwise, the lower left corner of the cohort B triangles would shift leftward as $n > 2$ increases. While the distinctly “do-or-die” flavor of this simple two period model exaggerates this desperate risk-taking effect, similar skewness-seeking behavior is often observed in lotteries (Yew Kwang 1965) or horse track betting (Golec and Tamarkin 1998).

The solution of this model for cohorts A and C is straightforward. The coin-toss gamble offers nothing in addition to the direct monetary gain or loss and is therefore unappealing to both, so $Y^{sA} = Y^{sC} = 0$. Cohort A will not reap any return on investment and hence has no incentive to invest, so $K^{sA} = 0$. Cohort C, on the other hand, has an incentive to invest provided $s$ and $r_1$ are sufficiently high. In particular, individuals in this cohort face the following simplified problem

\begin{equation}
\max_{K \in [0, W]} U = \ln(W + r_1H_1 - K) + \delta \ln(r_1(H_1 + sK))
\end{equation}

with necessary first order condition and $K^{sC}$ given by

\begin{equation}
\frac{\partial U}{\partial K} = \frac{-1}{W + r_1H_1 - K} + \frac{\delta r_1s}{r_1(H_1 + sK)} = 0
\end{equation}

\begin{equation}
K^{sC} = \frac{1}{1 + \delta} \left[ \delta W + (\delta r_1 - s^{-1})H_1 \right]
\end{equation}

As individuals in the desperate cohort B are still contemporaneously risk averse, they will only risk the minimum amount required to get them to $\bar{c}$ as determined by the distance between their current wealth and the threshold, adjusted for any investments in $K$. Thus, for this cohort $Y^{sB} = \bar{c} - (W + r_1H_1 - K)$ and the model becomes

\begin{equation}
\max_{K \in [0, W]} EU = 0.5 \ln(\bar{c}) + 0.5 \ln(2(W + r_1H_1 - K) - \bar{c}) + \delta[0.5 \ln(r_1(H_1 + sK))]
\end{equation}

1. This is true as long as the discount factor $\delta$ is not so small that the present value of a positive utility in Period 2 is trivial.

**FIGURE 1**

Graphical Depiction of Cohorts A, B, and C in Asset Space for Highest and Lowest Ability Types
with the solution for $K^{\ast B}$ given by

$$
\frac{\partial E}{\partial K} = -\frac{1}{2(W + r_iH_1 - K)} - \frac{0.5s}{r_i(H_1 + sK)} = 0 \partial \\
K^{\ast B} = \frac{1}{1 + \delta} [\delta W + (\delta r_i - s^{-1}) H_1 - 0.5s] = K^{\ast C} - \frac{0.5s}{1 + \delta}
$$

Optimal investment for the poorest individuals in cohort B, for whom $2W + r_iH_1 = \tau$, is

\[ K^{\ast B} |_{2W + r_iH_1 = \tau} = \frac{H_1}{1 + \delta} (1.5s - s^{-1}) \]

which marks the lower bound on investment for cohort B as $K^{\ast B}$ is increasing in $W$, $H_1$, and $r_i$. Thus, $K^{\ast B} > 0$ for all individuals in this desperate cohort for whom $r_i > (1.5s)^{-1}$. Investment levels for cohort B are lower than for cohort C because the threshold presents a relevant threat to asset preservation, which reduces the marginal value of investing by the 0.5 probability of not surviving to reap a return. While optimal investment is monotonically increasing in both $W$ and $H_1$ for both cohorts, moving from B to C across the boundary $W + r_iH_1 = \tau$ entails a discrete jump in optimal investment $K^{\ast}$. Figure 2 depicts the weakly monotone, discontinuous optimal investment schedule in $W$ and $H_1$ space assuming $r_i = (1.5s)^{-1}$ and $r_H > (1 + \delta)^{-1} + \delta s^{-1}$.

We can now compare two measures of risk aversion across the wealth distribution: the standard static coefficient of absolute risk aversion denoted as $SARA \equiv u''/u' = c_1^{-1} = (W + r_iH_1)^{-1} 2$ and a measure of dynamic risk aversion defined as $DRA \equiv -Y^*/W$. These measures are comparable in sign as risk-seeking (averse) behavior implies that both measures are negative (positive). In Figure 3, we depict $SARA$ and $DRA$ for the highest and lowest ability types with $H_1 = \overline{H}_{H}$ (see Figure 1). Over

2. In a purely static setting, $Y = K = 0$ so that $c_1 = W + r_iH_1$. 

### FIGURE 2
Optimal Human Capital Investment $K^{\ast}$ for Highest and Lowest Ability Types at (A)$\overline{H}_{H}$ and (B)$\overline{W}_{H}$ from Figure 1

![Figure 2](image)

### FIGURE 3
Absolute Risk Aversion and Dynamic Risk Aversion for Highest and Lowest Ability Types at $\overline{H}_{H}$ from Figure 1

![Figure 3](image)
the asset ranges corresponding to cohorts A and C, $DRA = 0$ and $SARA > 0$, and there is no dynamic risk response. But the presence and perception of nonconvex asset dynamics drive a wedge between static and dynamic risk aversion such that $SARA > 0$ and $DRA < 0$. Furthermore, these dynamics generate an observable behavioral response that suggests a locally inverse relationship between wealth and risk taking even though unobservable static risk preferences require the opposite. Finally, this model demonstrates the mitigating effect of ability on this desperate, dynamic risk response: high ability individuals exhibit dynamic risk taking over a lower and narrower range of wealth than do low ability individuals.

III. DISCUSSION

The observation that perceived dynamic asset thresholds can induce risk responses dates at least to Friedman and Savage’s (1948) classic article on risk and wealth, which hinted at this possibility by positing a wiggly utility curve. Instead of relegating it to the black box of preferences, we explicitly model this dynamic risk response by including nonconvex asset dynamics as a structural feature of intertemporal optimization. Making these dynamics explicit in models of decision making under risk draws a helpful distinction between static risk preferences and dynamic risk responses.

Our model assumes that individuals accurately perceive the location and severity of the critical dynamic threshold. This is an obvious necessary condition to any behavioral risk response to asset dynamics. The more precisely people perceive the dynamics of asset accumulation, the sharper will be the distinction between static and dynamic risk responses. Indeed, if people could perceive these dynamics perfectly—admittedly an extreme and unlikely case—two separate and relevant types of risk would emerge across all wealth levels: (1) static prospect risk associated with changes in wealth and (2) dynamic inertia risk associated with the forces on absolute wealth exerted by persistent, underlying dynamics. One could in principle decompose observed behavior into these components if the dynamics were understood well enough to be integrated as a structural feature of a model. Any unexplained behavior that remained after building in this structure might then offer a cleaner estimate of static risk preferences. Chevalier and Ellison (1997) address trade-offs between dynamic and static risk considerations empirically using data on mutual fund portfolios. They first estimate the dynamics of mutual fund size, then compare these dynamics to the risk-return trade-offs fund managers make. They find that fund managers tend to gamble with riskier fourth quarter portfolios in order to catch the market or make “best fund” lists. Surely such systematic and strategic trade-offs between static prospect risks and dynamic inertia risks are not confined to Wall Street and could be problematic in any empirical application that takes the standard static risk preference approach.

While it is unrealistic to expect individuals to perfectly perceive nonconvex asset dynamics that are far more subtle and complex than the stark threshold in this simple model, a growing body of empirical evidence suggests that in at least some contexts people indeed accurately perceive the location of critical thresholds in asset space. For example, Hoddinott (2006) finds that Zimbabwean households clearly behave as if a pair of oxen represents an asset threshold below which they strive not to fall. Santos and Barrett (2006), meanwhile, show that Ethiopian pastoralists’ subjective expectations of herd transitions conditional on rainfall realizations yield unconditional asset dynamics expectations virtually identical to those observed in separate herd history data from the same region (Lybbert et al. 2004). These studies suggest that people are more likely to perceive thresholds that occur at a clear discontinuity in asset space and that have severe, identifiable consequences. Contexts with nonconvex wealth dynamics, simple and discrete asset spaces, and discernible path dynamics with seasonal or annual—as opposed to daily or weekly—cash flows may be especially likely to evoke a dynamic risk response of the sort we model.

The notion of a poverty trap has long been a conceptual feature of development economics. More recently, rigorous theoretical models have shown that poverty traps can emerge when rational agents recognize various nonconvexities and market imperfections as part of the structure they face. Although it seems logical that agents may recognize a poverty trap itself as a structural feature and change their optimization behavior accordingly, many poverty trap models allow behavior to shape wealth dynamics but not the reverse. Thus, extreme risk aversion among the poor is commonly blamed for poverty traps without allowing these
traps to induce a risk response among them in return. In general, linkages between behavioral responses and wealth dynamics often seem to run in both directions. Making this two-way linkage more explicit could benefit both theoretical and empirical poverty trap research in such settings.

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